## Sequences and missing pieces

Today we will use our

- Problem solving and equation solving skills with sequence problems

Our main question "What am I missing?"

$$
t_{n}=a+(n-1) d
$$

1) In an arithmetic sequence $t_{95}=648.2$ and $t_{1}=9$, what is the common difference?

We know $a=9, n=95$ if $t_{n}=648.2$ so: $\quad 648.2=9+(95-1) d$

$$
639.2=94 d \quad d=6.8
$$

2) In an arithmetic sequence $t_{78}=48.7$ and $t_{79}=49.3$, what $t_{1}$ ?

We know $n=78$ if $t_{n}=48.7$ and $d=49.3-48.7 \quad$ so: $\quad 48.7=a+(78-1)(0.6)$
$48.7=a+46.2 \quad a=2.5$
3) How many terms? 12.8, 5, -2.8, ... -541

We know $a=12.8, d=5-12.8$ and $t_{\text {}}=$ so: $\quad-541=12.8+(n-1)(-7.8)$ $-553.8=-7.8(n-1)$ $71=n-1 \quad n=72$
4) In an arithmetic sequence $t_{96}=606.8$ and $t_{1}=14$, what is $t_{157}$ ?

We need 'd'
We know $a=14, n=96$ if $t_{96}=606.8$ so: $\quad 606.8=14+(96-1) d$

$$
\begin{aligned}
& 592.8=95 d \quad d=6.24 \\
& t_{157}=14+(157-1)(6.24)
\end{aligned} \quad t=987.44
$$

5) Fit 5 terms between 9 and 450 so that an arithmetic sequence is formed (these are called arithmetic means)

9
so 450 is the $7^{\text {th }}$ term 450
$450=9+(7-1) d$
$441=6 d$
$d=73.5$ now fill in blanks
982.5156229 .5303376 .5450

This missing pieces lesson will play a big part in our next 2 sequences lessons

Assignment $=$ worksheet

1) In an arithmetic sequence $\mathrm{t}_{16}=180$ and the common difference is 5.8 , find the first term.
2) In an arithmetic sequence $\mathrm{t}_{7}=434$ and the common difference is -82 , find the first term.
3) In an arithmetic sequence $t_{7}=18$ and $t_{1}=-66$, find the common difference.
4) In an arithmetic sequence $t_{64}=4$ and $t_{1}=100$, find the common difference.
5) How many terms are in the sequences below:
a) $10,15,20, \ldots . ., 250$
b) $1,4,7, \ldots, 121$
c) $\quad 40,38,36, \ldots .-290$
d) $-11,-7,-3, \ldots, 153$
e) $\quad 3,10.2,17.4, \ldots .413 .4$
f) $\quad 90,66,42, \ldots . .-1086$
6) In an arithmetic sequence $\mathrm{t}_{12}=66$ and the common difference is 7.8 , find $\mathrm{t}_{30}$.
7) In an arithmetic sequence $\mathrm{t}_{22}=74$ and the common difference is 4.8 , find $\mathrm{t}_{52}$.
8) In an arithmetic sequence $\mathrm{t}_{11}=68$ and $\mathrm{t}_{1}=-34$, find $\mathrm{t}_{100}$.
9) Fit 3 terms in-between 10 and 182 so that an arithmetic sequence is formed
10) Fit 4 terms in-between 99 and 15 so that an arithmetic sequence is formed
11) Fill in the blanks in the arithmetic sequences below
a) $\qquad$ , $\qquad$ , 14, $\qquad$ , 26
b) a) $\qquad$ , 3, $\qquad$ , $\qquad$ -18
12) Jar 1 contains 7 cookies, jar 2 contains 10 cookies, jar 3 contains 13 cookies ...
a) How many cookies are in jar 39?
b) Which jar contains 214 cookies?
