

## Discrete vs. Continuous Functions

In the function  $f(x) = mx + b$

The independent variable =  $x$  (we choose it)      Dependent variable =  $f(x)$  (we find it)

Reason: the value of  $f(x)$  **depends** on the  $x$  we choose

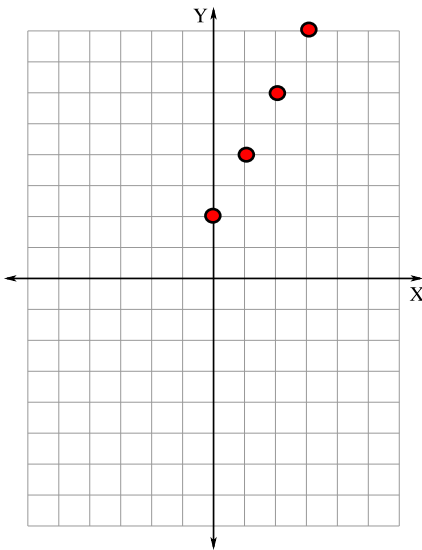
**Definitions:**

**Continuous function:**  $y$ 's exist for all real  $x$ -values (connect points with a continuous line)

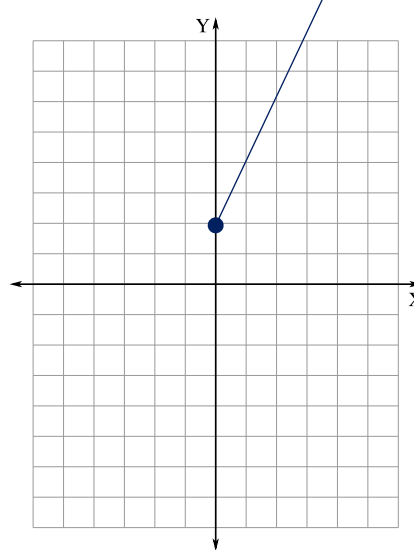
**Discrete Relation:** only whole #  $x$ 's exist ... so points cannot be connected by a line

Examples shown below

Discrete



Continuous



Stating the domain and range of a discrete function

Since only whole # values exist:      Domain:       $\{0, 1, 2, 3, 4 \dots\}$

Range:       $\{2, 4, 6, 8, 10, \dots\}$

*Seems like this function starts at 0*

If the domain and range don't continue to  $\infty$ , then you indicate largest value in domain and range.

Example: Cost of a pizza:  $c(t) = 1.5t + 12.50$  (maximum of 10 toppings)

<i>Creates the table</i>	<i>toppings</i>	$0$	$1$	$2$	$3$	$4 \dots$	$10 \text{ max}$
	<i>Cost:</i>	$12.50$	$14$	$15.50$	$17$	$18.50$	$27.50$

Domain:       $\{0, 1, 2, \dots, 10\}$

Range:       $\{12.5, 14, 15.5, \dots, 27.50\}$

(Why no negative  $x$ 's?)      **Can't have negative # of topping – 0 topping cheese pizza is smallest**

Would the following be discrete or continuous?

Cost to host a banquet per guest coming? since per guest = Discrete

Temperature of a hot coffee vs time? Temperature drops continuously

Height of a sunflower as it grows? Growth is continuous but a max and min exist

#of cookies in a cookie jar vs time? Per cookie = discrete

### Sketching functions

When the domain is any real #

Use your graphing rules

a)  $f(x) = \frac{2}{3}x + 5$       b)  $g(x) = \frac{-1}{4}x - 6$

y-int = 5, m = 2/3

y int = -6, m = -1/4

What if we fix the domain?

For example - if x represents time, or people

- Can't have neg x's, line has a starting point

c)  $f(x) = -2x + 1, \quad x \geq 0$

y int = 1, m = -2 but starts at x = 0

d)  $f(x) = \frac{2}{5}x - 3, \quad x > 0$

y int = -3, m = 2/5 but starts at x = 0 (hollow)

### Sketching Discrete Functions

Banquet Hall + Guests

Formula:  $C(t) = 15x + 250$       max 75 people

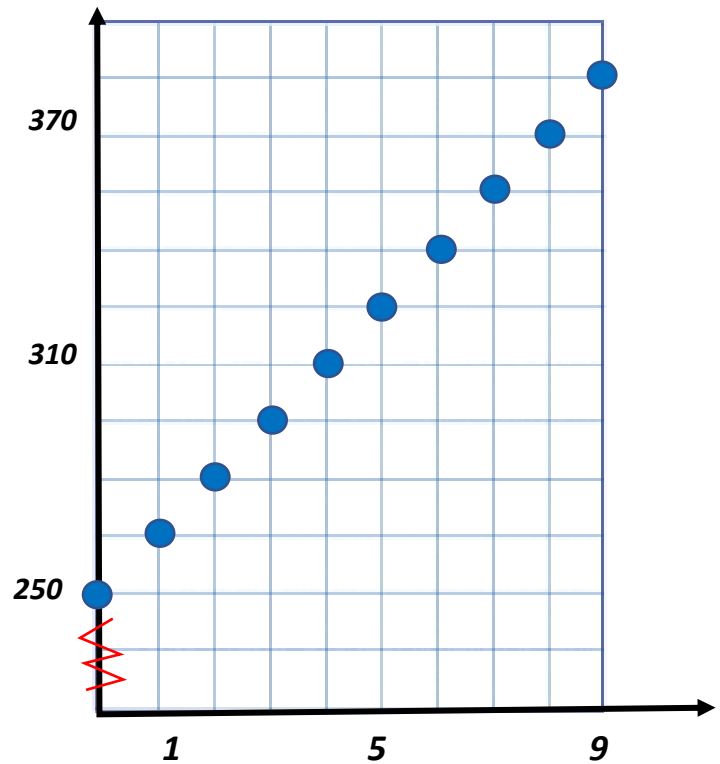
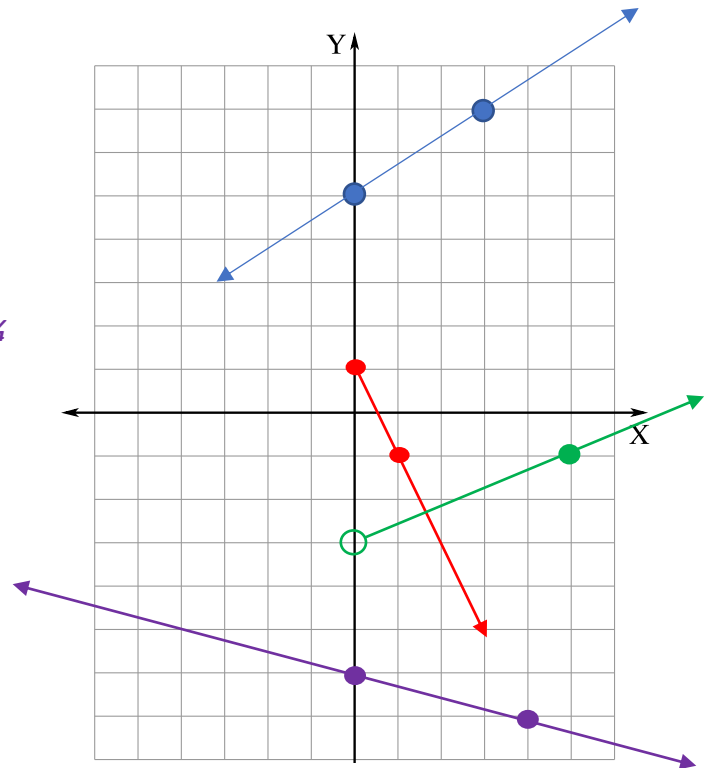
- y-int = 250, m = 15 (can't have negatives)
- the squiggle .... Allows me to not start at (0,0)

If the max number of people is 75,  
state the domain and range

D:  $\{0, 1, 2, 3, \dots, 75\}$

R:  $\{250, 265, 280, \dots, 1375\}$

Assignment = worksheet



### Sketching Functions - Continuous and Discrete

1) Sketch the 5 functions on the axis - the domain and range are all real numbers

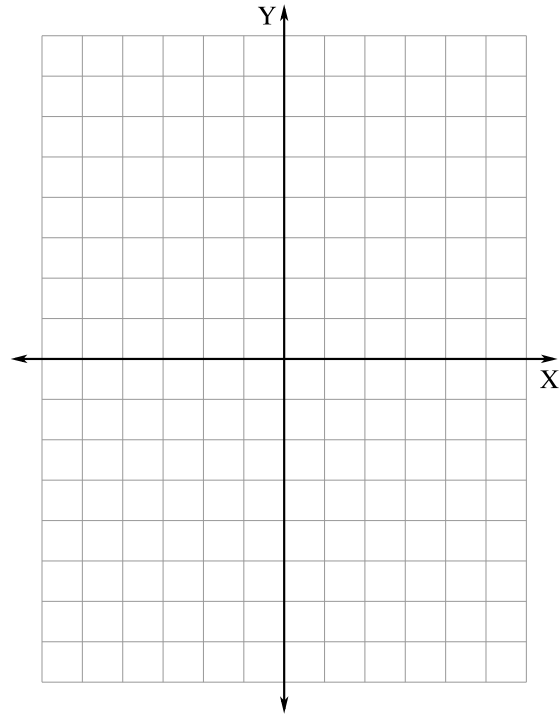
a)  $f(x) = 3x - 2$

b)  $g(x) = 4x + 1$

c)  $h(x) = \frac{3}{4}x - 7$

d)  $m(x) = \frac{-1}{5}x + 3$

e)  $q(x) = \frac{-1}{6}x$



2) Using the fixed domains, sketch the 5 functions on the axis provided.

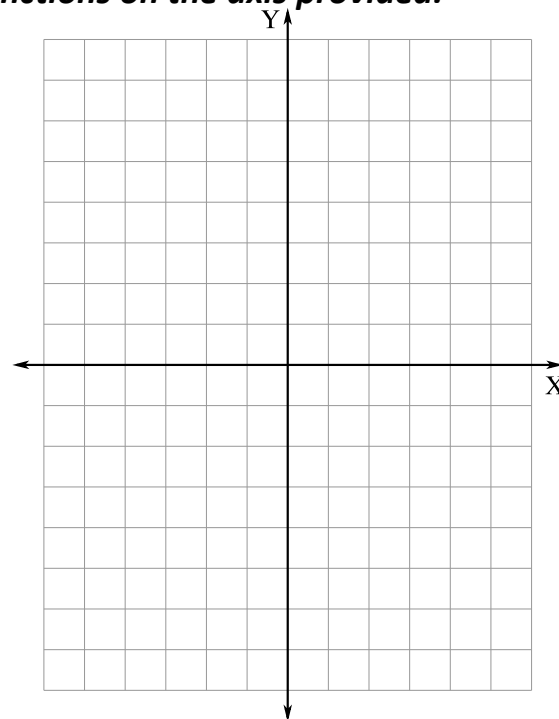
a)  $f(x) = 2x - 3, x \geq 0$

b)  $g(x) = -5x + 6, x > 0$

c)  $h(x) = \frac{3}{4}x - 5, x > 0$

d)  $n(x) = 3x - 8, x \geq 2$

e)  $p(x) = \frac{1}{3}x + 4, x > 3$



3) Determine if the following are discrete (D) or continuous (C)

a) temperature of a beaker of liquid vs time \_\_\_\_\_ b) height on a Ferris wheel vs time \_\_\_\_\_

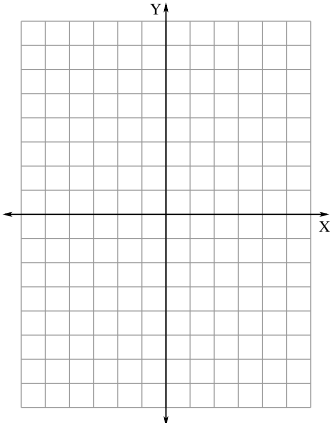
c) graphing money won vs tickets bought \_\_\_\_\_ d) your paychecks vs hours worked \_\_\_\_\_

e) bean length vs # of individuals \_\_\_\_

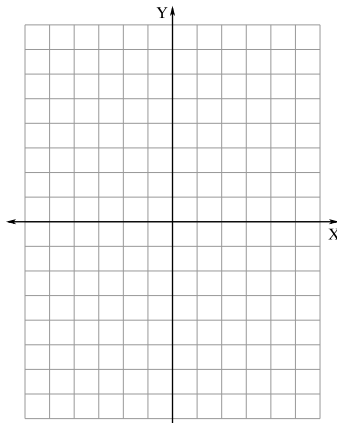
f) cost to rent a plumber if they charge for each  $\frac{1}{4}$  hour \_\_\_\_

4) Plot the following DISCRETE functions for  $\{0, 1, 2, 3, 4\}$  (Scale axis if needed)

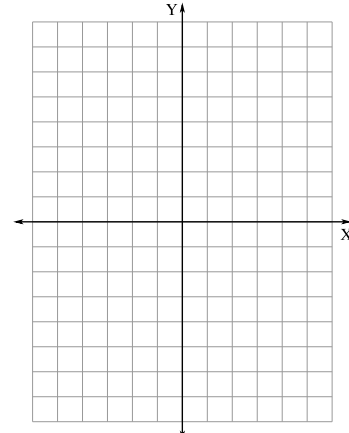
a)  $f(x) = 2x - 6$



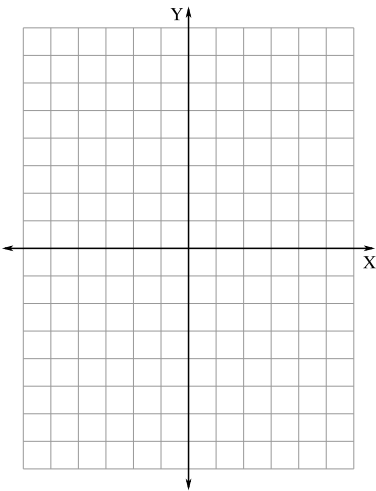
b)  $g(x) = -x + 7$



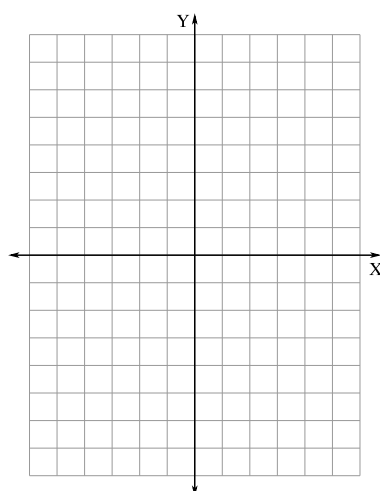
c)  $h(x) = 10x - 25$



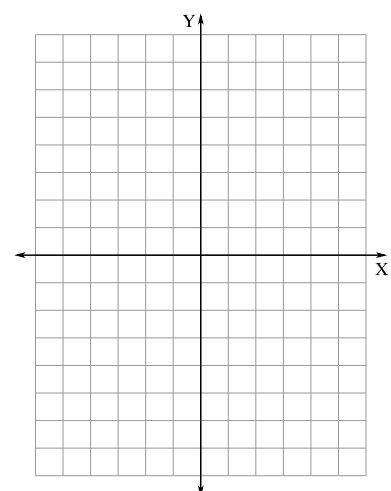
d)  $p(x) = \frac{1}{2}x + 2$



e)  $t(x) = -20x + 80$



f)  $k(x) = \frac{1}{2}x^2$



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4a) D:

R:

b) D:

R:

c) D:

R:

10a)

b)

c)

d)

12a)

b)

13a)

b)

c)