

FOM 11

5.5 Z – Scores

Since there are many different possible curves with different values of μ and σ , we can standardize the curve by transforming **each** score into a **z-score** (a measure of how many standard deviations a value is from the mean).

Standard Normal Distributions can be used in **every** problem for **any** data values.

Properties of a Standard Normal Distribution:

- Mean is 0.
- Standard Deviation is 1.
- Area under the curve is equal to 1.
- The graph is symmetrical about the mean.
- We use **z** instead of **x** to represent numbers along the horizontal axis.

$$z = \frac{x - \mu}{\sigma}$$

$$z = \frac{\text{term} - \text{mean}}{\text{standard deviation}}$$

- $A(z)$ is the **area under the curve to the left of z**.
- We can find the areas by using a graphing calculator or a z-table.

Example 1: If IQ scores are normally distributed with a mean of 100 and standard deviation of 15, determine:

- a. the z-score for 120.

$$z = \frac{x - \mu}{\sigma} = \frac{120 - 100}{15} = 1.33$$

- b. the probability that a randomly selected person has an IQ less than 120.

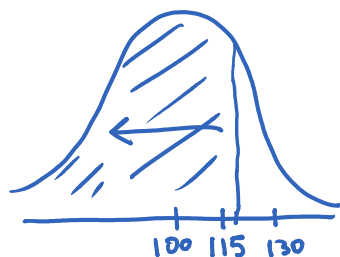
Find Area under the graph to left of 120 $A(z)$

$$z = 1.33$$

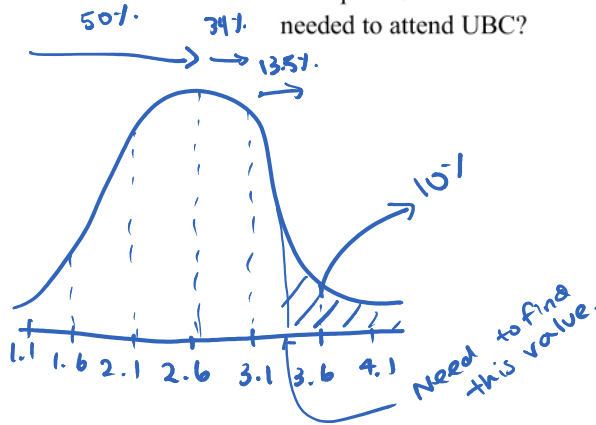
$A(1.33)$ find in z-tables pg 592-593

$$A(1.33) = 0.9082$$

$$= 90.82\% \text{ Probability}$$



Example 2: The GPA at GW Graham Secondary is 2.6, with a standard deviation of 0.5. If the top 10% of all students are eligible to attend UBC, what is the minimum GPA needed to attend UBC?



*Remember z-score tables give area to left of z.

Find value that gives area to left of 90%. (or closest to)

$$A(z) = 0.9000?$$

$$\text{Closest } A(1.28) = 0.8997$$

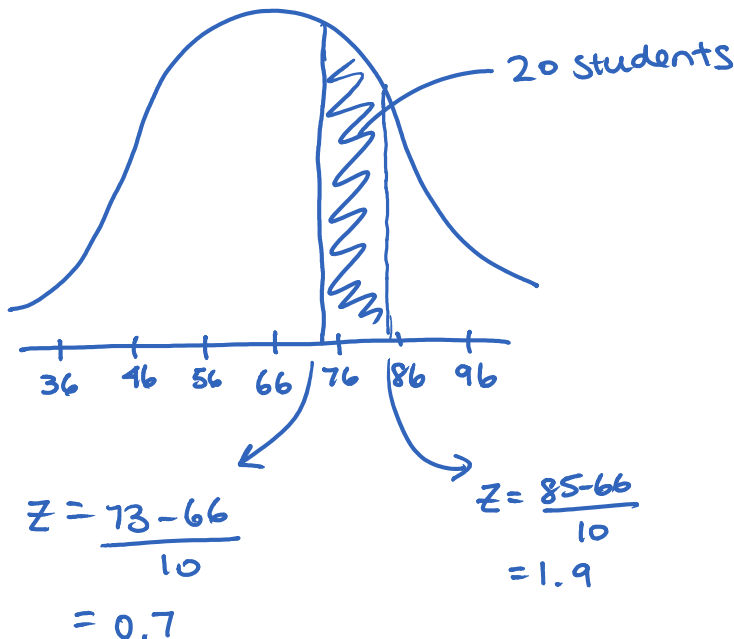
$$z = 1.28$$

$$z = \frac{x - \mu}{\sigma} \quad 1.28 = \frac{x - 2.6}{0.5}$$

$$0.64 = x - 2.6$$

$$\boxed{3.24 = x} \quad \leftarrow \text{minimum GPA}$$

Example 3: At a high school, the average grade for Science is 66, with a standard deviation of 10. If 20 students with grades between 73 and 85 receive B's, how many students are taking Science at the high school?



Percent between 73 & 85

$$A(1.9) - A(0.7)$$

$$A(1.9) = 0.9713 = 97.13\%$$

$$A(0.7) = 0.7580 = 75.8\%$$

$$97.13 - 75.8 = 21.33\%$$

$$\frac{20 \text{ students}}{x} = \frac{0.2133}{1}$$

$$x = 93.765$$

94 students take science.

omit

Example 4: A manufacturer of cell phones has determined a mean of 26 months before a need of repairs, with a standard deviation of 6 months. What length of time for this warranty should the manufacturer set so that less than 10% of all cell phones will need repairs during the warranty period?

~~Assignment: Pg. 264 #5-7(ac), 8, 9, 11, 13-15, 17, 20~~

HW p.264 #5-7(ac), 8, 9, 11, 15, 17