

Equations of Parallel and Perpendicular Lines

To finish the unit we will write the equations of parallel and perpendicular lines.
This will require us to steal a slope from a given equation and find a new y-intercept

1) Find the equation of a line, in slope intercept form,

a) parallel to $y = \frac{1}{3}x - 7$ passing thru (27, 11)

$$\text{parallel} \rightarrow m = \frac{1}{3} \text{ for our new line} \quad y = \frac{1}{3}x + b \quad \rightarrow \quad 11 = \frac{1}{3}(27) + b$$

$$11 = 9 + b \quad \rightarrow \quad y = \frac{1}{3}x + 2$$

b) perpendicular to $y = \frac{-2}{5}x + 7$ passing thru (8, 15)

$$\text{perp} \rightarrow m = \frac{5}{2} \text{ for our new line} \quad y = \frac{5}{2}x + b \quad \rightarrow \quad 15 = \frac{5}{2}(8) + b$$

$$15 = 20 + b \quad \rightarrow \quad y = \frac{5}{2}x - 5$$

c) perpendicular to $6x - 7y = 14$ with the same y-intercept

$$6x - 14 = 7y \quad \rightarrow \quad y = \frac{6}{7}x - \frac{14}{7} \quad \text{perp} \rightarrow m = \frac{-7}{6} \text{ for our new line and } b = -2$$

$$y = \frac{-7}{6}x - 2$$

2) Use pt-slope form to write the equation of a line

a) parallel to $11x - 5y - 10 = 0$ passing thru (19, -5)

$$11x - 10 = 5y \quad \rightarrow \quad y = \frac{11}{5}x - \frac{10}{5} \quad \text{parallel} \rightarrow m = \frac{11}{5} \text{ for our new line}$$

$$y + 5 = \frac{11}{5}(x - 19)$$

b) perpendicular to $9y + 4x = 11$ passing thru the x-intercept of $6x - 5y = 18$

$$9y = -4x + 11 \quad y = \frac{-4}{9}x + \frac{11}{9} \quad \text{perp} \rightarrow m = \frac{9}{4} \text{ for our new line}$$

$$6x - 5y = 18 \quad \text{if } y = 0, x = 3 \quad y + 0 = \frac{9}{4}(x - 3)$$

Assignment = worksheet

Parallel and perpendicular Lines Worksheet

Use slope y-intercept form for #1 to 7

- 1) Find the equation of the line that is parallel to $y = 8x - 6$ passing through $(-4, 12)$

- 2) Find the equation of a line perpendicular to a line of slope 4 passing through $(-4, 10)$

- 3) Find the equation of a line perpendicular to $y = -2x + 6$ passing through $(-8, 8)$

- 4) Find the equation of a line parallel to $y = -7x + 12$ passing through $(7, 3)$

- 5) Find the equation of a line perpendicular to $y = \frac{-1x}{3} + 6$ passing through $(11, -6)$

- 6) Find the equation of a line parallel to $y = -4x + 10$ passing through $(1, 10)$

- 7) Find the equation of a line perpendicular to $y = \frac{-4x}{3} + 7$ passing through $(2, -10)$

Use point slope form for #'s 8 thru 11

8) Find the equation of a line parallel to $6x + y = 10$ passing through $(12, -6)$

9) Find the equation of a line parallel to $7x + y = 10$ passing through $(14, -8)$

10) Find the equation of a line perpendicular to $6x + y = 19$ passing through $(18, 0)$

11) Find the equation of the line perpendicular to $8x - y = 10$ but passing through the y-intercept of $6x + y = 19$

Use slope y-intercept for the last 2 questions

12) Find the equation of the line perpendicular to $2x - y = 20$ but passing through the x-intercept of $19x - 6y = -18$.

13) Find the equation of the line parallel to $12x - 6y = 19$ but passing through the x-intercept of $5x - 3y = -10$.

You should also try Page 374 #20(a), 21, 22, 24 (use point slope form for all of these)