Slope
4 types of slope exist:


Slope is also called"rate of change"

Slope is calculated by measuring the rise over run

Making a formula:


To get the rise we subtracted the y's, to get the run we subtracted the $x$ 's (but in same order)


They represent $2^{\text {nd }} y$ minus $1^{\text {st }} \boldsymbol{y}$
Some examples:

1) Find the slope between
a) $M(5,3)$ and $Y(8,2)$
$m=\frac{2-3}{8-5} \quad$ or $\quad m=\frac{-1}{3} \quad$ Notice order: $\quad m=\frac{3-2}{5-8} \quad$ or $\quad m=\frac{1}{-3}$
b) $\mathrm{O}(-7,4)$ and $\mathrm{H}(3,10)$

$$
m=\frac{10-4}{3--7} \quad \text { or } \quad m=\frac{6}{10} \quad \text { or } \quad \frac{3}{5}
$$

c) $Y(8,2)$ and $E(8,-7)$

$$
m=\frac{-7-2}{8-8} \quad \text { or } \quad m=\frac{-9}{0} \text { this is an undefined slope (can't divide by } 0 \text { ) }
$$

d) $A(-7,-3)$ and $H(-6,-20)$

$$
m=\frac{-20--3}{-6--7} \quad \text { or } \quad m=\frac{-17}{1} \quad \text { or }-17
$$

2) State the slope of lines shown
a) flat line $m=0$
b) Find 2 good points rise $=2$, run $=3 \quad m=\frac{2}{3}$
c) For this line only $\mathbf{2}$ good points exist


$$
m=\frac{-11}{9}
$$

3) Point R(4, -2) lines on a line with a slope of $1 / 4$, state 2 other points on this line

Rise $=1$ run $=4$ so add 1 to $y$ and add 4 to $x$ and you can generate as many points as needed
$(4,-2)$
$\rightarrow \quad(8,-1)$
$\rightarrow \quad(12,0)$
(or subtract ... (0, -3)
4) The slope containing ( $-8,3$ ) and $(k, 2)$ is $\frac{3}{5}$ Find $k$
$\frac{3}{5}=\frac{2-3}{k-8} \quad \rightarrow \quad \frac{3}{5}=\frac{-1}{k+8} \quad \rightarrow \quad 3 k+24=-5 \quad$ solve for $k \quad k=\frac{-29}{3}$
5) Suppose a trench needs to have a slope of 0.35 over a horizontal distance of 6.4 m . How many cm will the trench drop in this span?
$6.4 \mathrm{~m}=640 \mathrm{~cm}$
$0.35=\frac{\text { rise }}{640} \quad$ rise $=224 \mathrm{~cm}$

Cross off answers as you find them

(2)

(3)

(4)


9)
$(1,-4) ;(6,-2)$
(6)

10) $(-3,1) ;(-7,4)$
14) $(1,-1) ;(-2,-6)$
15) $(-4,-8) ;(-2,0)$
16) $(-3,-3) ;(0,0)$
13) $(0,-1) ;(4,-7)$
7) $(2,1) ;(5,3)$
11) $(9,2) ;(3,-1)$
12) $(-5,8) ;(-4,2)$
8) $(8,3)$; $(2,5)$
17) $(2,5) ;(9,1) \quad(0,0) ;(-2,7)$

| DU | AB | CK | ST | AR | IG | AT | OB | IG | ET | BE | ST |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | -6 | $-\frac{3}{5}$ | $-\frac{4}{7}$ | 9 | $\frac{1}{2}$ | $-\frac{7}{2}$ | $-\frac{7}{6}$ | $\frac{4}{3}$ | $\frac{2}{3}$ | $-\frac{5}{4}$ | $\frac{5}{3}$ |
| CA | RD | RI | CH | UC | RI | ME | AQ | UA | KY | ET | CK |
| $\frac{2}{5}$ | $\frac{1}{6}$ | $-\frac{1}{4}$ | -2 | -8 | $-\frac{3}{2}$ | 1 | $-\frac{1}{3}$ | $-\frac{3}{4}$ | $\frac{8}{5}$ | 4 | 3 |

What you might have if you don't feel well?

|  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $-\frac{4}{3}$ | $-\frac{1}{2}$ | $\frac{3}{7}$ | 1 | -2 | $\frac{2}{3}$ | -3 | $\frac{7}{3}$ | 4 | $-\frac{5}{2}$ | 0 |

O) $(3,-3)$ and $(4,1)$
S) $(-2,4)$ and (0, -2)
N) $(-5,2)$ and ( $-3,-3$ )
O) $(0,-1)$ and (4, 3)
V) $(-1,0)$ and $(-3,4)$

Now complete Page 340
6a) rise $=$

$$
\text { Run }={ }^{m=}
$$

b) rise =
c) $\quad$ rise $=$ $m=$ run $=$

7a)
b)
b)

8a)
c)
c)
d)

11a)
b)

15a)
b)

17a)
b)
c)
d)

